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$$

- What happens as $t \to \infty$?

- Part 2 (Rakotomalala & dW, in review, 2026):

- What about existence of spots and lanes?

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